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McAfee

CURRENT FLOW IN A THIN FILM CADMIUM SULFIDE DIODE.

Thesis M12



# CURRENT FLOW IN A THIN FILM CADMIUM SULFIDE DIODE

by

ROBERT EARL MCAFEE

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B.S., U. S. Naval Academy
(1960)

SUBMITTED IN PARTIAL FULFILLMENT OF THE REQUIREMENTS FOR THE DEGREE OF

MASTER OF SCIENCE

at the

MASSACHUSETTS INSTITUTE OF TECHNOLOGY June, 1963

Signature of Author
Department of Electrical Engineering, May 17, 1963

Certified by

Accepted by
Chairman, Departmental Committee on Graduate Students

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CURRENT FLOW IN A TALE FILM CADMIUM SULFIELD DIOLY

by

#### ROBERT EARL MOAFEE

Submitted to the Department of Electrical Engineering on May 17, 1963, in partial fulfillment of the requirements for the degree of Master of Science.

### ABSTRACT

Dictes were prepared using thin films of cadmium sulfide sandwiched between thin-films, metal electrodes. The current versus voltage characteristics were studied as a function of the manufacturing process and temperature. The variables in the manufacturing process were choice of metals for electrodes, interchange of top and bettom electrode, deposition of an exide barrier between electrode and insulator, heat treatment of the cadmium sulfide, and variation of the substrate temperature during deposition. From the results obtained, space-charge-limited currents could not be the physical mechanism involved. Instead an argument could be made for a field emission phenomenon at low temperatures with Schottky emission occuring at higher temperatures. The two regions were separated by a sharp transition at a critical temperature.

Thesis Supervisor: James G. Gottling Title: Assistant Professor of Electrical Engineering

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## ACKNOWLEDGEMENT

J. G. Gottling of the Department of Electrical Engineering for not only the idea behind this thesis, but also for many helpful suggestions along the way. The author is also indebted to Professor M. S. Osmon, J. D. Heightley, and P. Thiesen for constructive criticism and help in some of the experimental techniques. Last, but not lesst, the author is indebted to his wife who listened patiently to all the failures, cheered for all the successes, and finally typed the finished copy.

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## TABLE OF CONTENTS

Title Page	t de la companya de l
Abstract	2
Aoknowledgement	3
Table of Contents	Žļ
List of Illustrations	5
I. Introduction	6
II. Experimental	8
III. Discussion	13
IV. Conclusion	19
Appendix	50
References	30

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	This of Chargerone
	In Introduction
	Lar make pri + 17
	colorand Call
	W. confinite
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180	Today make

## LIST OF ILLUSTRATIONS

1.	Physical design of diode	8a
5.	V-1 characteristics of 2145	පීම.
3.	Static V-1 characteristics of 2145	අපි
4.	Variation of characteristics with oxide thickness	109
5.	Log I vs 1/T for 2154	<b>10</b> a
6.	Log (1-1 <sub>0</sub> /T <sup>2</sup> ) vs 1/T for 2154	<b>11</b> a
7.	Log I vs V <sup>2</sup> for 2154	110.
8.	Bend model	<b>21</b> a
9.	Lindmayer, Reynolds, and Wrigley curve	21a
10.	Limiting values of Log J vs Log V	298

#### I. INTRODUCTION

Thin film diodes composed of a metal electrode-cadmium sulfide-metal electrode sandwich were evaporated on to a glass substrate with the purpose of obtaining a solid-state analog to a vacuum diode. The theory of space-charge-limited currents in insulators plus the experimentally observed space-charge-limited currents in single crystal of cadmium sulfide seemed to indicate that such a thin-film device might be feasible. Rectification properties of similar diodes have been observed previously, but little is known about the physical processes involved.

Dresner and Shallcross<sup>8</sup> attempted to describe the phenomenon as a space-charge-limited current, but were not successful. They found a large discrepancy between the density of traps as indicated by theory and as measured by the method of thermally stimulated currents. The measured density of  $10^{21}/\text{cm}^3$  seems more reasonable than the calculated density of  $10^{13}/\text{cm}^3$  assuming the i-v relationship was space-charge-limited. Single crystals of cadmium gulfide have been observed to have a trap density of  $10^{14}/\text{cm}^3$ .

A second point of major difference was the measured capacitance. Lampert has shown that the maximum deviation from the geometrical capacitance is a multiplicative factor

<sup>1.</sup> Superscripts refer to references at the end of this paper.

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of two for space-charge-limited currents. Dreamer and Shalloress were unable to observe a capacitance of less than four times the geometric capacitance.

No conclude that space-charge-limited current alone cannot be the basis for this device. This project had as its main purpose the determination of some kind of model for the current flow process. No conclusive answer was reached, but a conjecture as to the correct model was made. First, Schottky emission is dominant at temperatures elevated above a critical temperature and second, below this critical temperature, the dominant process is field emission or tunneling. The critical temperature was observed only experimentally and could not be explained by the theory.

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#### II. EXPERIMENTAL

The diodes were prepared by the evaporation of electrodes and the cadmium sulfide on glass microscope slides. The geometry employed in all samples is shown in figure 1. The method of preparing the slides for deposition has been described by Caman. During the deposition process, the pressure in the vacuum system was held in the neighborhood of 10°5 torr.

The cadmium sulfide used was laboratory grade powder manufactured by B & A Company. This powder was evaporated from open molybdenum boats. At first the substrates were cooled with liquid nitrogen in order to speed the rate of condensation of CdS. It was later found, however, that the resistivity of the films was greatly increased by heating the substrates to 150°C. Several workers have reported using higher substrate temperatures, and one paper reports obtaining resistivities of thin-film cadmium sulfide approaching that of the single crystaline material.

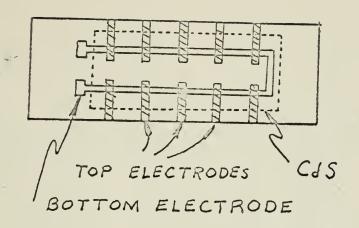
It was found in the earlier work that some of the samples prepared on the cold substrates were chinic immediately after manufacture. These could be made non-linear by heating in an oven at temperatures of 100-200°C for periods of several hours. This process is similar to that described by Dresner and Shalloross.

511de 2145 had aluminum as the bottom (common) electrode

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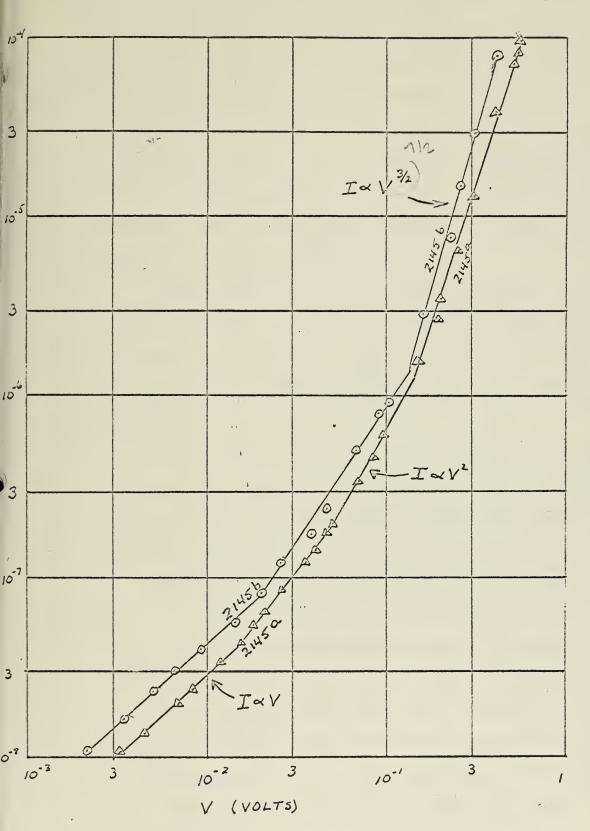
## FIGURE 1

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FIGURE 2

1: -8a-





I-V CHARACTERISTICS 2145 FORWARD CURRENT

FIGURE 3



and gold for the top electrode. The cadmium sulfide was evaporated onto a cold substrate and then annealed in vacuum for 20 minutes prior to the addition of the gold. The average thickness of the film as determined by optical interference methods was 1120°A. All ten diodes had rectifying properties similar to those shown in figure 2. In all cases the gold electrode was the anode for forward conduction. The cadmium sulfide was markedly photosensitive.

Figure 3 shows static 1-v characteristics obtained from 2145a and 2145b. Notice that a region of chmic dependence followed by a square-law region was observed. Above this, however, a region of I av 7/2 was observed. This is not easily explained.

Sample 2146 was constructed as nearly 2145 as possible.

No non-linear characteristics were observed. The measured average thickness of the cedmium sulfide was 1160°A. The maximum observed deviation from this thickness was 180°A.

Sample 2154 was made with two gold electrodes. The last 20% of the bottom electrode and the initial part of the cadmium sulfide were evaporated simultaneously to produce a region of forced diffusion. No attempt was made to determine the exact thickness of this mixed layer. Some recatifying characteristics were noted with the bottom electrode positive for forward bias.

In sample 2166, the electrodes were again aluminum and gold. When the sample was first made, a-c characteristics were photographed from the oscilloscope plot. All diodes

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indicated that gold was the anode for forward current. Several days later, after 2166a was held at 13 volts a-c for several minutes, it was noticed that aluminum had become the anode for forward currents. It was suspected that high fields caused the change.

When 2167 was made, all of the diedes had aluminum as the anode. This raised the possibility of an exide film effect since it is well known that aluminum exidizes rapidly even at pressures of 10<sup>-5</sup> torr. It was also noted that the current remained small until the voltage was approximately one volt. Then the current increased rapidly with increasing voltage. When 7 volts a-c was applied, this slide became too hot to touch. No such heating effects were noticed on any other sample.

The results of 2167 suggested making a dicde with the aluminum electrode purposely exidized in varying amounts to determine the effect of exide thickness. 2168 was constructed with two dicdes anodized to each of the following voltages in a pH 3.0 solution of tartaric acid: 0, 1, 2, 3, and 4 volts. Figure 4 shows the variation of the a-c characteristics with exide thickness. Notice that the thicker the exide, the higher the voltage threshold in the forward direction.

The Fowler-Nordheim equation for field emission is well known and may be given by the approximate expression: 12

$$J = I(E) \exp \left[ \frac{-8\pi}{3h} (2me)^{\frac{1}{2}} \frac{4^{\frac{3}{2}}}{E} \right]$$
 (1)

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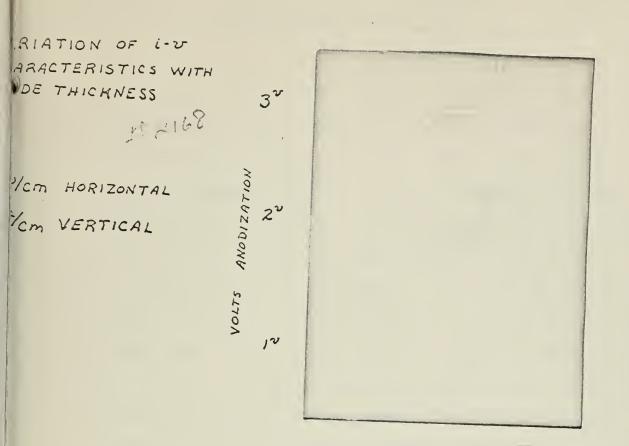
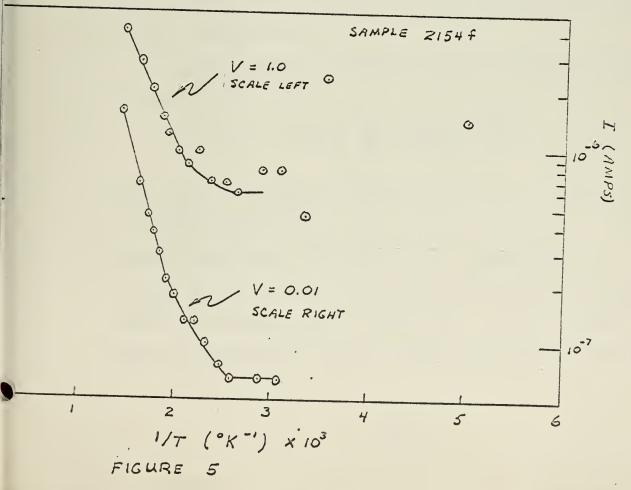


FIGURE 4





$$J \approx I(\mathcal{E}) \exp\left[-6 \times 10^9 \frac{\mathcal{Q}^{3/2}}{\mathcal{E}}\right]$$
 (2)

where  $I(E) = 1.55 \times 10^{-6} E^2/\varphi$ , E is the electric field strength in volts / meter,  $\varphi$  is the work function in electron volts. As can be seen from (1), E must be quite large before any appreciable current will flow. However, once this threshold field is reached, the current may be expected to increase as  $E^2$ . This appears to be the case in figure 4.

The current was measured as a function of temperature with the voltage as a parameter for samples 21340, 2134d, 2154f, and 2154g. The results of these are shown in figure 5. A region of the curve exhibits an essentially temperature independent portion located below a critical temperature. In an effort to determine whether Schottky emission was present, a curve of  $\log \left[ (I - I_c) / T^2 \right]$  versus 1/T was plotted and is shown in figure 6. (In is the constant current below the critical temperature.)

Schottky emission ourrent-voltage-temperature relation is given by: 13

$$J = R T^2 exp \left[ \frac{\varphi}{k} - C \left( \frac{Y}{Ka} \right)^{n/2} \right] / T$$
 (3)

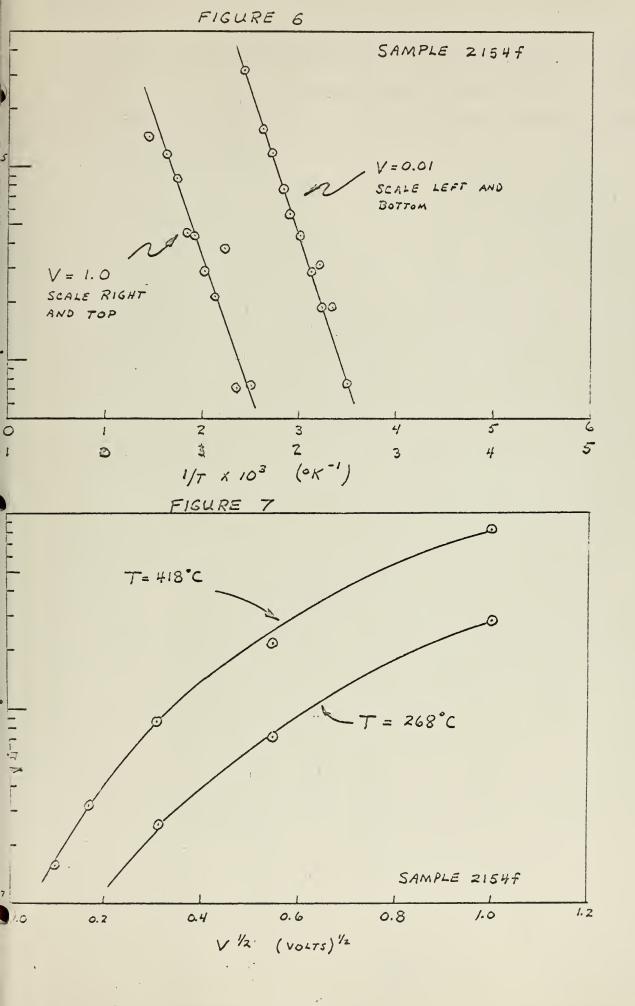
where R is Richardson's constant,  $\varphi$  the work function, K the dielectric permittivity, and a the film thickness. C is a constant whose value is 4.389 for V in volts and a in centimeters. From (3) it is evident that the curves of figure 6 should be straight lines as they are. It would appear that Schottky emission was present above the critical temperature.

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This case differs from field emission in that it is temperature dependent and does not set in until some elevated temperature is reached. The field emission data was measured at room temperature. The same at all the last of the same at th

Dresner and Shallorose have pointed out the difficulties of explaining the current process as a space-charge-limited phenomenon. This author found one difficulty they did not mention. The current varying as the 7/2 power of the voltage in the high current region is difficult to explain using sol currents. Rose has shown that it is possible to obtain  $I \sim V (T^{\circ}/T + 1)$  for an exponential distribution of traps with energy, but Dresner and Shalloross did not observe such a distribution. A rough calculation by this author based on assuming an impulse distribution of traps at .35 eV below the conduction band gave a square law dependence. Lot us follow through this calculation.

We know that the density of trapped electrons, 77% is given by

$$n_t = \frac{N_t}{l + \frac{N_c}{n} e^{-\epsilon_t/RT}}$$
 (4)

where Nt is the density of trapping states located Et below the conduction band. For the approximation given in equation (26), Appendix to hold, we must have

$$\frac{Nc}{m} \gg exp(Et/kT)$$
 (5)

If (5) is true, then (26), Appendix is true, and as the results in the Appendix show, J must then be proportional to  $v^2$ . We can demonstrate that (5) is true for the present

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problem.

For the drift limited approximation,

$$J = me \mathcal{L} = constant.$$
 (6)

Lampert<sup>2</sup> has shown that the maximum deviation of  $\varepsilon$  from the average field strength  $|\varepsilon|$  is at most a factor of two. Therefore, we can use (6) together with the experimentally observed values of J and  $|\varepsilon|$  to get the maximum value of J. In our case  $J_{max} \approx 10^{-1}$  amps/om<sup>2</sup> with  $|\varepsilon|_{max} = 10^{-1} = 0$  amps/om<sup>2</sup> with  $|\varepsilon|_{max} = 10^{-1} = 0$ . If we assume a mobility of 4 cm/volt-sec, then m is approximately  $10^{-1}/cm3$ . No =  $10^{-1}$  at room temperature which gives  $10^{-1}/cm3$ . No =  $10^{-1}$  at room temperature which gives  $10^{-1}/cm3$ . On  $10^{-1}/cm3$  at room temperature which gives  $10^{-1}/cm3$ . On  $10^{-1}/cm3$  at room temperature which gives  $10^{-1}/cm3$  and  $10^{-1}/cm3$  are  $10^{-1}/cm3$ . Therefore (5) holds and J should be proportional to  $10^{-1}/cm3$ .

We can demonstrate that we have chosen the worst possible case; ie, the case where (5) is the least likely to be valid. If (5) holds for the maximum J, then it must hold for all smaller J values because from (6), n would be even smaller. If  $\triangle$  is larger than the small value (judging from normal values measured in single crystals), then again n is smaller. Therefore, we conclude that J should be proportional to  $V^2$  and should not have a  $J \propto V^{7/2}$  range which was observed.

We can make a few remarks about using the exponential trap distribution of Rose. First, as we mentioned above, the measured trapping density was not exponential, Second, we can show that if the exponential distribution does hold, then at constant voltage, current should increase with decreasing temperature. We will use Rose's calculations, but will fill

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in the constant he did not state except to say that it was a function of temperature. Rose defined

$$\mathcal{M}_t = A \exp\left(-E_t / k T_c\right) \tag{7}$$

where A is a constant and the other symbols are as before. The condensed charge forced into the insulator is

$$Q = CV \tag{8}$$

where C is the capacitance. This condensed charge raises the Fermi level by an amount E defined by the relation

$$\int_{E_f - \Delta E}^{E_f} A \exp(-E_L/kT) dE = \frac{CV}{e}$$
 (9)

The solution of this equation (neglecting the upper limit) is:

$$\Delta E = kT_{c}(lnV + K)$$
 (20)

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$$K = ln \left( \frac{C}{AekT_c} \right) + \frac{E_f}{kT_c}$$
 (11)

If we define as the ratio of free to total charge, we can write

$$\Theta = \frac{eN_c}{CV} \exp\left(-\frac{E_f}{kT} + \Delta E/kT\right)$$
 (12)

where No is the effective density of states in the conduction band. If we use (10) for E, then

$$\Theta = \frac{e N_c}{c V} \left[ V^{\frac{T_c}{T}} \left( \frac{c}{A e k T_c} \right)^{T_c} \right]$$
 (13)

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We now use equation (25) from the Appendix which may be written as

$$J = \frac{9}{8} \frac{\epsilon_{\Theta M}}{J^2} V^2 \tag{34}$$

It can be seen from equation (22), the appendix that the in (14) is the same as (13). Therefore we have

$$J = (constant) V^{\frac{T_c}{f}+1} \left(\frac{C}{AekT_c}\right)^{\frac{C}{f}}$$
 (15)

which verifies our statement that the current increases with decreasing temperature. This was not observed experimentally. On the contrary, the opposite effect was noted.

From the two calculations we have just made, we must conclude that space-charge-limited currents alone cannot explain the experimentally observed facts. We must seek other physical processes to explain the data. Two which came to mind were field emission and Schottky emission.

rield emission seemed a likely candidate when it was noted that the diodes had a very sharp voltage threshold for conduction with the aluminum positive. The Fowler-Nordheim equation is given by (2). If we assume an oxide thickness of 10°A which we postulate as having been insdvertantly created on the aluminum electrical during the manufacturing process, we can demonstrate that a voltage threshold would exist. For E < 10°7 volts/cm, the exponential term in (2) is vanishingly small. As a matter of fact, E must be of the order of 10°6 volts/cm before the current density approaches 10°6 amps/cm². A field of 10°8 volts/cm in the present case corresponds to a

Alternative and product will be a larger to the control of the con

 terminal voltage of 1 volt providing all of the field is across the exide.

The results obtained by purposely cridizing the aluminum show conclusively that oxide does have an effect on the current characteristics. However, the results are insufficient to show indisputably that field emission is present. Instead, we can only remark that the observed shifting of the voltage threshold value with increased oxide thickness is indicative of field emission and the the magnitude of this threshold is approximately correct,

We can make a fairly strong case for Schotthy emission. Figure 5 indicates a definite temperature dependance of the ourrent above a certain critical temperature. Below this oritical temperature, the current is relatively temperature independent. This type of behavior is suggestive of Schottky emission. Reference to (3) shows that if Schottky emission is the dominant physical process we should expect plots of log I versus  $V^{\frac{1}{2}}$  and  $\log [(I-I_0)/7^2]$  versus 1/T to be straight lines. These plots are shown in figures 6 and 7. In figure 6. We see that we have a fairly straight line, especially at higher values of T (lower values of 1/T). The erratic part of the line tends to be at the low temperature end. This is because at this end of the curve. Io played a significant role, Any inaccuracy in the determination of Io would affect the curve radically. At the other end, however, Io was almost negligible in comparison with I and hence, any inaccuracy in

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In figure 7, it is difficult to account for the observed curve. As stated above, we expect a straight line if Schottky emission was present. We could not offer any explanation, and for this reason we were unable to conclude that Schottky emission was definitely observed.

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 In attempting to draw some conclusions from the data, this author was forced to make only a conjecture since conclusive evidence was not available. It is suggested that both field emission and Schottky emission occur in the dicke. In the high temperature region, Schottky emission is dominant and in the low temperature region tunneling occurs. Space-charge-limited currents can be ruled out. Further experiments are necessary to pin down definitely the physical processes that were observed.

The experiments that this author considers need to be done are the following:

- (a) Make several samples with varying oxide thicknesses and measure i-v characteristics at different temperatures with the purpose of looking for Schottky emission above the critical temperature.
- (b) Use a higher vacuum system to attempt to eliminate the inadvertant formation of oxide on the aluminum.
- (c) Conduct noise measurements on the sample to obtain further evidence of the lack of space charge current. This situation would be indicated if a failure to observe space charge suppression of noise.
- (d) Conduct a thermal determination of density of trapping states.
- (e) Measure the capacitance of the samples with different bias values.

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### APPEND IX

## SPACE-CHARGE-LIMITED CURRENTS IN SOLIDS

Space Charge Limited Currents (SCLC) in insulators have been investigated theoretically by a number of workers. The first results of any consequence was the derivation of the Child-Langmuir Law for a trap-free insulator by Mott and Currey. Following their work, (but using the mathematical convention of Lampert, et al. that  $\vec{E} = -\vec{E} \hat{\lambda}$ ,  $\vec{J} = -\vec{J} \hat{\lambda}$ ,  $\vec{A} \vec{E} = \frac{dV}{J \times}$  we first write the general current flow equation:

$$J = neu \mathcal{E} - e D \frac{dn}{dx}, \qquad (1)$$

where J is the current density, n is the electron density, a is the magnitude of the electronic charge, is the mobility, E is the electric field strength, and D is the diffusion constant for electrons. Then in addition we have Poisson's equation:

$$\frac{dE}{dx} = \frac{me}{E},$$
 (2)

where & is the dielectric constant of the material.

In an insulator, we assume that the diffusion component of the current is negligible in comparison with the drift component, ie, (1) becomes:

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If we carry out the integration of (1) and (3) we obtain

$$\mathcal{E} = \pm \left(\frac{2J_X}{\epsilon u} + \text{constant}\right)^{1/2}$$
 (4)

To evaluate the constant we must use an appropriate boundary condition. We assume that this is 2-0 at X=0. Reference to figure 8 shows that this is equivalent to having the cathode at  $X=X_0$ . If  $X_0$  is small in comparison with the thickness of the insulator, then the assumption of the boundary condition is valid. The negative sign in (4) may be discarded as is obvious from either (3) or the figure.

To relate the applied voltage to the observed current we integrate (4)

$$V - \frac{\varphi_2 - \varphi}{e} = \int_0^d E d\pi = -\frac{2}{3} \left(\frac{2J}{Eu}\right)^{1/2} d^{3/2}$$
 (5)

or in terms of i= - JA we have

$$i = \frac{9}{8} \frac{\epsilon \mu A}{d^3} \left( Y - V_0 \right)^2 \tag{6}$$

where  $V_0 = \frac{\rho_2 - \rho_1}{c}$ ,  $\rho_2$  is the work function of the anode, and  $\rho$ , is the work function of the cathode. This result is the Child-Langmuir law for solids. We see that it differs from the vacuum law primarily by a factor of  $V^2$  instead of  $V^3/2$ .

This result has geveral serious difficulties as was pointed out by Lempert, and clarified considerably by Lindmayer. Reynolds, and Wrigley. We have assumed that T=0 at X=0. But if this is true, then (3) telle us that J(0)=0 or J=0 everywhere since the current is constant. Also the problem

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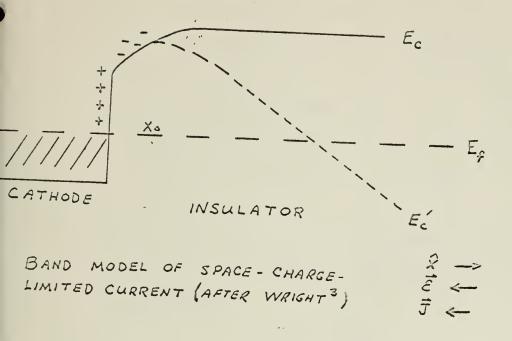


FIGURE 8

SOLUTION OF THE SPACE CHARGE PROBLEM INCLUDING DIFFUSION ACCORDING TO LINDMAYER, REYNOLDS, AND WRIGLEY "

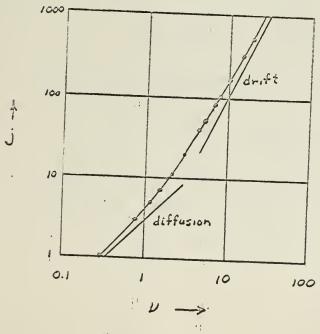


FIGURE 9



has two natural boundary conditions, one at X=0 and one at X=d. In the above discussion we have only used the one at X=0. The trouble comes in neglecting the diffusion current. Lindmayer, et al. have solved the complete problem which we shall give here for convenience.

First let us combine (1) and (2) to obtain

$$J = \epsilon u \mathcal{E} \mathcal{E}' - \epsilon D \mathcal{E}'' \tag{7}$$

where the primed quantities indicate differentiation with respect to X. We simplify this equation by the use of the normalizations:

$$S = \frac{\pi}{d}$$

$$F = -udE/D$$

$$J = ud^3 J/E D^2$$
(8)

to obtain:

$$j = F'' + \frac{(F^2)'}{2}$$
 (9)

Integrating once

$$5j+C_1 = F' + \frac{F^2}{2}$$
 (10)

Now if the substitution F = 2u'/u is made we have

$$u'' = (C, +5j)u/2$$
 (11)

which is an ordinary, linear differential equation. We simplify (11) even farther by making the change of variable

$$3 = -(C_1 + 5j)/(2j^2)/3$$
 (22)

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(60) (2[2]/(82-1) = E

The result is

$$\frac{d^2u}{dz^2} + zu = 0 \tag{23}$$

This equation has a solution of the form  $U = R_i f_i + k_1 f_2$  where the k's are arbitrary constants. As Lindmayer, et al. have pointed out, the apparent three constants are in reality only two. This may be seen by calculating the normalized potential, V,

$$V = \frac{gV}{hT} = \int_{0}^{1} FdS = 2\int_{0}^{1} \frac{u'}{u} = 2\ln\frac{u(1)}{u(0)},$$
 (14)

where we have used the Einstein relation  $\frac{D}{dx} = \frac{kT}{2}$ . Now putting the general solution into (14) we have the result that

$$y = 2 \ln \left\{ \frac{k_i f_i(i) + k_2 f_2(i)}{k_i f_i(0) + k_2 f_2(0)} \right\} = 2 \ln \left\{ \frac{f_1(i) + C_2 f_2(i)}{f_i(0) + C_2 f_2(0)} \right\}$$
(25)

It is now apparent that only two constants exist.

The solution to (13) is known in the form of an infinite series and is given by Lindmayer, et al. This solution, however, is not one that allows a straight-forward application of the boundary conditions, since the constants C<sub>1</sub> and C<sub>2</sub> are buried in the series. The boundary conditions may be applied by use of a computer trial and error process. Before we look at the results of this computation, let us determine the appropriate boundary conditions to use.

If we consider a physical structure with a material sandwiched between an anode and a cathode, then the boundary condition at X=d (the anode) or S=1 is

$$F'(1) = 0$$
 or  $uu'' = (u')^2$  (16)

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if we assume that all electrons arriving at the ancde are swept away by the field.

The boundary conditions at X=0 or S=0 is less apparent.

We first assume that the electric field here is equal to zero.

We see that since we have included the diffusion component of the current as well as the drift component, this boundary condition no longer leads to zero current as previously. Hence, we take as our second boundary condition

$$F(0)=0$$
 or  $u_{s=0}^{d}=0$  (27)

The results obtained by Lindmayer, Reynolds, and Wrigley are shown in figure 9.

ourrent (or j) is low, then we assume a diffusion limited situation. If this is so then (9) becomes

$$j = F_{j}^{"} \tag{18}$$

which has a solution

$$\mathbf{j} = 3\mathbf{\nu} \tag{19}$$

Figure & shows this solution plotted in comparison with the complete solution. Also shown is the drift limited case.

Calculating the transition for high values of j is difficult. Lindmayer, et al. found that  $f_1(0)$  and  $C_2f_2(0)$  in (15) form a difference with variation only in the eighth significant figure for values of j > 600. But by calculating F

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point by point and starting at both boundaries, they were able to project the curve to  $j=10^4$ . Up to this limit the series solution appears to be approaching the drift limited case. The error is below 10% in the drift limited approximation for  $V>100\,\mathrm{kT}/9$ .

The work of Lindmayer, et al. appears to give justification for our previous assumption that the diffusion ourrent could be neglected as long as  $V > 100 \, kT/g$  in the case of a trap-free structure. We shall assume that it is likewise justified to make the same assumption in the case of trapping. If we neglect diffusion, then the equations we must solve are:

$$\frac{dE}{dx} = \frac{(n+n_t)e}{\epsilon}$$
 (20)

$$J = neu \mathcal{E}$$
 (21)

where n is the density of free carriers, nt is the density of trapped carriers, and the other symbols are as before. If we define

$$\Theta \equiv \frac{m}{m_t m_t} \tag{22}$$

and substitute for n + nt in (20) we have

$$\frac{\epsilon\Theta}{e}\frac{d\epsilon}{dx}=n \tag{23}$$

which may be substituted into (21) which gives:

$$J = \epsilon u \Theta \mathcal{E} \frac{d\mathcal{E}}{dx} \tag{24}$$

If 6 is independent of x, then the solution of (24) is

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the same as (6) with OM substituted for Mor

$$i = \frac{9}{8} \frac{\epsilon \Theta u A}{d^3} \left( V - V_0 \right)^2. \tag{25}$$

6 is given approximately by

$$\Theta = \frac{N_c}{N_t} \exp\left(-E_t/kT\right) \neq \Theta(x) \tag{25}$$

for the case of a single level of shallow traps whose density is Nt and whose distance below the conduction band is  $E_t$ . No is  $10^{19}$  at room temperature. For  $N_t = 10^{17}$  and  $E_t = 0.5$  volt,  $\Theta = 10^{-7}$  and space-charge-limited currents are greatly reduced.

In general, we cannot assume  $\Theta \neq \Theta(x)$  as was done above. The exact mathematical solution becomes very complicated if not impossible to carry out. Before we attempt to do more with the solution, let us examine some of the characteristics of the problem and see what can be learned without a rigorous solution.

The problem we are solving is the set of equations (20) and (21) plus the fact that we assume n and  $n_{\hat{c}}$  are specified by the normal Fermi statistics. We can write the equation relating n(x) to  $E_r$ , the fermi energy as:

where Nc is the effective density of states in the conduction band at temperature T and Ec(x) is the lower edge of the conduction band. When a set of traps of density N<sub>t</sub> at energy  $E_t(x)$  are in quasi-equilibrium with n(x), then

(M-1) / 1-1 (M-1) (M-1)

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$$m_t(x) = N_t \{ 1 + \exp([E_t(x) - E_f(x)]/kT) \}^{-1}$$

$$= m(x) N_t \{ m(x) + N \}^{-1}$$
(28)

The boundary condition we assume is as before EmO at XmO.

Following Lampert we can make some very general observations about the set of equations. In the neutral crystal, (ie, no injected charge) ohm's law must hold. This follows because Poisson's equation becomes

$$\frac{dE}{dx} = 0 \tag{29}$$

but since J is a constant,

$$\frac{dJ}{dx} = 0 = neu \frac{dE}{dx} + eu E \frac{dn}{dx}$$
 (30)

The first term on the right in (30) is zero from (29). Therefore, the second term on the right is zero. This implies dn/dx=0 or  $n=n_0$  is a constant independent of x. We may then define  $neu = \sigma$  and Ohm's law results.

Ohm's law and Child's law curves intersect when the excess injected carrier density at the ancde calculated from Child's law becomes similar to 70., the neutral carrier density. We can find the voltage, Va, at which the crossover occurs by equating the chmic current to the space-charge-limited current,

$$J_{a} = e n_{o} u \frac{V_{a}}{d} = J_{scl} = \frac{9}{8} \frac{\epsilon u}{d^{3}} V_{a}^{2}$$
 (31)

which gives

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$$V_a = \frac{8}{9} \frac{e n_o d^3}{\epsilon}. \tag{32}$$

Let us now examine the situation when all of the traps within the insulator are filled. We shall find that this gives us a third limit on our J-V characteristics.

When all of the traps are filled, then there is an unneutralized charge present in the insulator that tends to prevent additional charge injection. The voltage is necessary to overcome the repulsion from the charge condensed in the traps. Let us follow the mathematics through for this case in more detail.

If all of the traps are filled, then  $n_t\!=\!\!N_t$  and Poisson's equation becomes

$$\frac{dE}{dx} = (m+N_t) \frac{e}{e}. \tag{33}$$

We now substitute (33) in (30) and use ( ) to obtain a nonlinear differential equation in n as

$$\frac{dm}{dx} + n^3 \frac{e^2 u}{\epsilon J} + n^2 \frac{N_t e^2 u}{J} = 0$$
 (34)

This equation is separable and the integral in n is tabulated.
Using the boundary condition that at X=0 gives

$$X = \left(\frac{\epsilon J}{N_t e^2 u}\right) \frac{1}{n} - \left(\frac{\epsilon J}{N_t^2 e^2 u}\right) \ln \left(1 + \frac{N_t e^2 u}{\epsilon J}\right)$$
 (35)

or with n eliminated,

$$X = \frac{\mathcal{E}}{eNt} - \frac{\mathcal{E}J}{e^2N_t^2u} \ln\left(1 + \frac{eN_tu}{J}\mathcal{E}\right)$$
 (36)

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Using the voltage definition

$$V(x) = \int_{0}^{x} \mathcal{E}(x) \frac{dx}{d\mathcal{E}} d\mathcal{E}, \qquad (37)$$

we have

$$V(x) = \frac{\varepsilon}{eN_t} \left[ \frac{\varepsilon^2(x)}{2} - \frac{J}{eN_t u} + \frac{J^2}{e^2 N_t^2 u^2} l_n \left( 1 + \frac{eNtu}{J} \varepsilon \right) \right]$$
(38)

(36) and (38) do not form a very tractable set of parametric equations, but a J vs V(d) relation may be obtained by assuming a J in (36) and solving for E(d). This value of E(d) is substituted into (38) to obtain V(d). This has been done by Heightley for the case  $N_t = 10^{17}/cm^3$ ,  $M = 200 \text{ cm}^2/volt - sec$ ,  $\epsilon = 1160$ ,  $\epsilon = 10^{17}/cm^3$ ,  $\epsilon = 10^{17}/cm^3$ ,  $\epsilon = 10^{17}/cm^3$ .

In figure 17, we see a triangle formed by Ohm's law.

Child's law for solids, and the traps-filled-limit (TFL) law.

We state that the J-V curve must lie within this triangle

because:

- (a) J cannot lie below Chars law since carriers injected at the cathode can only enhance the current flow.
- (b) J cannot lie above Child's law since this represents the case where all injected carriers add to the current flow.
- (c) J cannot lie below TFL law since this represents the case when the least number of injected carriers contribute to the current.

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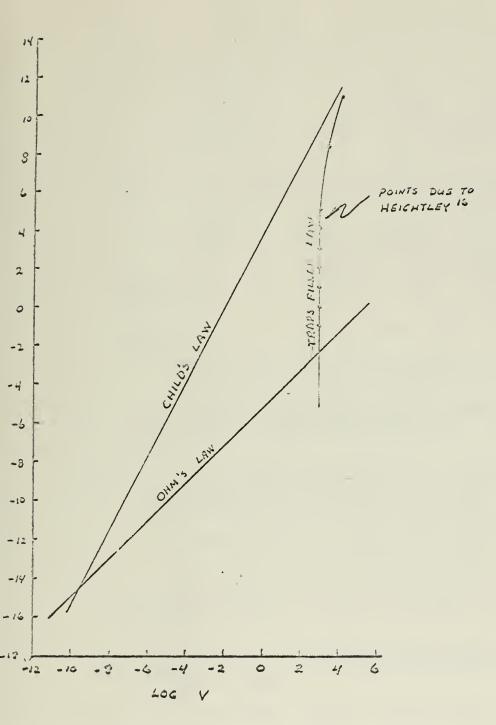
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LIMITING LOG J VS LOG V CHARACTERISTICS
FOR SPACE-CHARGE-LIMITED CURRENT WITH TRAPS

FIGURE 10



#### REFERENCES

- 1. A. Rose, Phys. Rev., 97, 1538 (1955).
- 2. M. A. Lampert, Phys. Rev., 103, 1649 (1956).
- 3. G. T. Wright, Proc. I.E.E., 106B, 915 (1959).
- 4. J. Lindmayer, J. Reynolds, & C. Wrigley, J. Appl. Phys. 34, 809 (1963).
- 5. For a brief summary of references 1-4, see Appendix of this paper.
- 6. R. W. Smith & A. Rose, Phys. Rev., 97, 1531 (1955).
- 7. J. W. Mac Arthur, Electrical Properties of Thin Films of CdS, (Report 7848 7849 R 4, Servemechanisms Laboratory, MIT, Cambridge, 1958), pp 29-36.
- 8. J. Dresner & F. V. Shallcross, Solid-State Elect. 5, 205 (1962).
- 9. R. H. Bube, Phys. Rev. 99, 1105 (1955).
- 10. M. S. Osman, A Mechanism for 1/f Noise of Thin Evaporated Metal Films, (Report ESL-R-149, MIT, Cambridge, 1962).

  p 49.
- 11. K. Weiss, Gorman Patent 837,424. Fatent desgribes process of obtaining specific resistances of 10 1010 A -cm with substrate temperatures from 380°C to 420°C.
- 12. T. J. Lewis, Phys. Rev. 101, 1694 (1956).
- 13. S. R. Pollack, J. Appl. Phys. 34, 877 (1963).
- 14. Lampert has shown that the maximum deviation from the average field is a factor of 2. (See reference 2.)
- 15. N. F. Mott and R. W. Gurney, <u>Electronic Processes in Ionic Crystals</u> (Cxford University Press, New York, 1940), first edition, p. 172.
- 16. J. D. Heightley, Private Communication.

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